

# Simulation study on improved Shapiro-Wilk test of normality

**Zofia Hanusz and Joanna Tarasińska**

*University of Life Sciences in Lublin, Poland*

## Abstract

The  $W$  statistic proposed by Shapiro and Wilk ([2]) is frequently used for testing of the univariate and multivariate normality. However, the table of coefficients in the  $W$  statistic, its critical values and also constants in Johnson's  $S_B$  transformation to normal distribution ([3]), are not correct. Royston ([1]) gave an approximation for coefficients in the  $W$  statistic and use them to evaluate proper critical values of the Shapiro-Wilk test. In the paper, we determine new constants for the  $W$  statistic and Johnson's  $S_B$  transformation. Empirical significant levels of the improved Shapiro-Wilk test and the power against chosen alternatives are evaluated via simulation study.

## Keywords

Multivariate normality, Empirical significant level, Power of the test.

## References

- [1] Royston, P. (1992). Approximating the Shapiro-Wilk  $W$ -test for non-normality. *Stat. Comput.* 2, 117–119.
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- [3] Shapiro, S.S. and M.B. Wilk (1968). Approximations for the null distribution of the  $W$  statistic. *Technometrics* 10, 861–866.